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Angela Dean  
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# Design and Analysis of Experiments

*Second Edition*

 Springer

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# Design and Analysis of Experiments

Second Edition

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## Preface to the Second Edition

Since writing the first edition of *Design and Analysis of Experiments*, there have been a number of additions to the research investigator's toolbox. In this second edition, we have incorporated a few of these modern topics.

Small screening designs are now becoming prevalent in industry for aiding the search for a few influential factors from amongst a large pool of factors of potential interest. In Chap. 15, we have expanded the material on saturated designs and introduced the topic of *supersaturated designs* which have fewer observations than the number of factors being investigated. We have illustrated that useful information can be gleaned about influential factors through the use of supersaturated designs even though their contrast estimators are correlated. When curvature is of interest, we have described *definitive screening designs* which have only recently been introduced in the literature, and which allow second order effects to be measured while retaining independence of linear main effects and requiring barely more than twice as many observations as factors.

Another modern set of tools, now used widely in areas such as biomedical and materials engineering, the physical sciences, and the life sciences, is that of *computer experiments*. To give a flavor of this topic, a new Chap. 20 has been added. Computer experiments are typically used when a mathematical description of a physical process is available, but a physical experiment cannot be run for ethical or cost reasons. We have discussed the major issues in both the design and analysis of computer experiments. While the complete treatment of the theoretical background for the analysis is beyond the scope of this book, we have provided enough technical details of the statistical model, as well as an intuitive explanation, to make the analysis accessible to the intended reader. We have also provided computer code needed for both design and analysis.

Chapter 19 has been expanded to include two new experiments involving split-plot designs from the discipline of human factors engineering. In one case, imbalance due to lost data, coupled with a mixed model, motivates introduction of restricted-maximum-likelihood-based methods implemented in the computer software sections, including a comparison of these methods to those based on least squares estimation.

It is now the case that analysis of variance and computation of confidence intervals is almost exclusively done by computer and rarely by hand. However, we have retained the basic material on these topics since it is

fundamental to the understanding of computer output. We have removed some of the more specialized details of least squares estimates from Chaps. 10–12 and canonical analysis details in Chap. 16, relying on the computer software sections to illustrate these.

SAS® software is still used widely in industry, but many university departments now teach the analysis of data using R (R Development Core Team, 2017). This is a command line software for statistical computing and graphics that is freely available on the web. Consequently, we have made a major addition to the book by including sections illustrating the use of R software for each chapter. These sections run parallel to the “Using SAS Software” sections, retained from the first edition.

A few additions have been made to the “Using SAS Software” sections. For example, in Chap. 11, PROC OPTEX has been included for generation of efficient block designs. PROC MIXED is utilized in Chap. 5 to implement Satterthwaite’s method, and also in Chaps. 17–19 to estimate standard errors involving composite variance estimates, and in Chap. 19 to implement *restricted maximum likelihood estimation* given imbalanced data and mixed models.

We have updated the SAS output<sup>1</sup>, showing this as reproductions of PC output windows generated by each program. The SAS programs presented can be run on a PC or in a command line environment such as unix, although the latter would use PROC PLOT rather than the graphics PROC SGPLOT.

Some minor modifications have been made to a few other chapters from the first edition. For example, for assessing which contrasts are non-negligible in single replicate or fractional factorial experiments, we have replaced normal probability plots by *half-normal probability plots* (Chaps. 7, 13 and 15). The reason for this change is that contrast signs are dependent upon which level of the factor is labeled as the high level and which is labeled as the low level. Half-normal plots remove this potential arbitrariness by plotting the absolute values of the contrast estimates against “half-normal scores”.

Section 7.6 in the first edition on the control of noise variability and Taguchi experiments has been removed, while the corresponding material in Chap. 15 has been expanded. On teaching the material, we found it preferable to have information on mixed arrays, product arrays, and their analysis, in one location. The selection of multiple comparison methods in Chap. 4 has been shortened to include only those methods that were used constantly throughout the book. Thus, we removed the method of multiple comparisons with the best, which was not illustrated often; however, this method remains appropriate and valid for many situations in practice.

Some of the worked examples in Chap. 10 have been replaced with newer experiments, and new worked examples added to Chaps. 15 and 19. Some new exercises have been added to many chapters. These either replace

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<sup>1</sup>The output in our “Using SAS Software” sections was generated using SAS software Version 9.3 of the SAS System for PC. Copyright © SAS 2012 SAS Institute Inc. SAS and all other SAS Institute Inc. product or service names are registered trademarks or trademarks of SAS Institute Inc., Cary, NC, USA.



exercises from the first edition or have been added at the end of the exercise list. All other first edition exercises retain their same numbers in this second edition.

A new website <http://www.wright.edu/~dan.voss/DeanVossDraguljic.html> has been set up for the second edition. This contains material similar to that on the website for the first edition, including datasets for examples and exercises, SAS and R programs, and any corrections.

We continue to owe a debt of gratitude to many. We extend our thanks to all the many students at The Ohio State University and Wright State University who provided imaginative and interesting experiments and gave us permission to include their projects. We thank all the readers who notified us of errors in the first edition and we hope that we have remembered to include all the corrections. We will be equally grateful to readers of the second edition for notifying us of any newly introduced errors. We are indebted to Russell Lenth for updating the R package `lsmeans` to encompass all the multiple comparisons procedures used in this book. We are grateful to the editorial staff at Springer, especially Rebekah McClure and Hannah Bracken, who were always available to give advice and answer our questions quickly and in detail.

Finally, we extend our love and gratitude to Jeff, Nancy, Tom, Jimmy, Linda, Luka, Nikola, Marija and Anika.

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Dayton, USA  
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## Preface to the First Edition

The initial motivation for writing this book was the observation from various students that the subject of design and analysis of experiments can seem like “a bunch of miscellaneous topics.” We believe that the identification of the objectives of the experiment and the practical considerations governing the design form the heart of the subject matter and serve as the link between the various analytical techniques. We also believe that learning about design and analysis of experiments is best achieved by the planning, running, and analyzing of a simple experiment.

With these considerations in mind, we have included throughout the book the details of the planning stage of several experiments that were run in the course of teaching our classes. The experiments were run by students in statistics and the applied sciences and are sufficiently simple that it is possible to discuss the planning of the entire experiment in a few pages, and the procedures can be reproduced by readers of the book. In each of these experiments, we had access to the investigators’ actual report, including the difficulties they came across and how they decided on the treatment factors, the needed number of observations, and the layout of the design. In the later chapters, we have included details of a number of published experiments. The outlines of many other student and published experiments appear as exercises at the ends of the chapters.

Complementing the practical aspects of the design are the statistical aspects of the analysis. We have developed the theory of estimable functions and analysis of variance with some care, but at a low mathematical level. Formulae are provided for almost all analyses so that the statistical methods can be well understood, related design issues can be discussed, and computations can be done by hand in order to check computer output.

We recommend the use of a sophisticated statistical package in conjunction with the book. Use of software helps to focus attention on the statistical issues rather than the calculation. Our particular preference is for the SAS software, and we have included the elementary use of this package at the end of most chapters. Many of the SAS program files and data sets used in the book can be found at [www.springer-ny.com](http://www.springer-ny.com). However, the book can equally well be used with any other statistical package. Availability of statistical software has also helped shape the book in that we can discuss more complicated analyses—the analysis of unbalanced designs, for example.



The level of presentation of material is intended to make the book accessible to a wide audience. Standard linear models under normality are used for all analyses. We have avoided using calculus, except in a few optional sections where least squares estimators are obtained. We have also avoided using linear algebra, except in an optional section on the canonical analysis of second-order response surface designs. Contrast coefficients are listed in the form of a vector, but these are interpreted merely as a list of coefficients.

This book reflects a number of personal preferences. First and foremost, we have not put side conditions on the parameters in our models. The reason for this is threefold. Firstly, when side conditions are added to the model, all the parameters appear to be estimable. Consequently, one loses the perspective that in factorial experiments, main effects can be interpreted only as averages over any interactions that happen to be present. Secondly, the side conditions that are the most useful for hand calculation do not coincide with those used by the SAS software. Thirdly, if one feeds a nonestimable parametric function into a computer program such as PROC GLM in SAS, the program will declare the function to be “nonestimable,” and the user needs to be able to interpret this statement. A consequence is that the traditional solutions to the normal equations do not arise naturally. Since the traditional solutions are for nonestimable parameters, we have tried to avoid giving these, and instead have focused on the estimation of functions of  $E[Y]$ , all of which are estimable.

We have concentrated on the use of prespecified models and preplanned analyses rather than exploratory data analysis. We have emphasized the experimentwise control of error rates and confidence levels rather than individual error rates and confidence levels.

We rely upon residual plots rather than formal tests to assess model assumptions. This is because of the additional information provided by residual plots when model assumption violations are indicated. For example, plots to check homogeneity of variance also indicate when a variance-stabilizing transformation should be effective. Likewise, nonlinear patterns in a normal probability plot may indicate whether inferences under normality are likely to be liberal or conservative. Except for some tests for lack of fit, we have, in fact, omitted all details of formal testing for model assumptions, even though they are readily available in many computer packages.

The book starts with basic principles and techniques of experimental design and analysis of experiments. It provides a checklist for the planning of experiments, and covers analysis of variance, inferences for treatment contrasts, regression, and analysis of covariance. These basics are then applied in a wide variety of settings. Designs covered include completely randomized designs, complete and incomplete block designs, row-column designs, single replicate designs with confounding, fractional factorial designs, response surface designs, and designs involving nested factors and factors with random effects, including split-plot designs.

In the last few years, “Taguchi methods” have become very popular for industrial experimentation, and we have incorporated some of these ideas. Rather than separating Taguchi methods as special topics, we have interspersed

them throughout the chapters via the notion of including “noise factors” in an experiment and analyzing the variability of the response as the noise factors vary.

We have introduced factorial experiments as early as Chapter 3, but analyzed them as one-way layouts (i.e., using a cell means model). The purpose is to avoid introducing factorial experiments halfway through the book as a totally new topic, and to emphasize that many factorial experiments are run as completely randomized designs. We have analyzed contrasts in a two-factor experiment both via the usual two-way analysis of variance model (where the contrasts are in terms of the main effect and interaction parameters) and also via a cell-means model (where the contrasts are in terms of the treatment combination parameters). The purpose of this is to lay the groundwork for Chapters 13–15, where these contrasts are used in confounding and fractions. It is also the traditional notation used in conjunction with Taguchi methods.

The book is not all-inclusive. For example, we do not cover recovery of interblock information for incomplete block designs with random block effects. We do not provide extensive tables of incomplete block designs. Also, careful coverage of unbalanced models involving random effects is beyond our scope. Finally, inclusion of SAS graphics is limited to low-resolution plots.

The book has been classroom tested successfully over the past five years at The Ohio State University, Wright State University, and Kenyon College, for junior and senior undergraduate students majoring in a variety of fields, first-year graduate students in statistics, and senior graduate students in the applied sciences. These three institutions are somewhat different. The Ohio State University is a large land-grant university offering degrees through the Ph.D., Wright State University is a mid-sized university with few Ph.D. programs, and Kenyon College is a liberal arts undergraduate college. Below we describe typical syllabi that have been used.

At OSU, classes meet for five hours per week for ten weeks. A typical class is composed of 35 students, about a third of whom are graduate students in the applied statistics master’s program. The remaining students are undergraduates in the mathematical sciences or graduate students in industrial engineering, biomedical engineering, and various applied sciences. The somewhat ambitious syllabus covers Chapters 1–7 and 10, Sections 11.1–11.4, and Chapters 13, 15, and 17. Students taking these classes plan, run, and analyze their own experiments, usually in a team of four or five students from several different departments. This project serves the function of giving statisticians the opportunity of working with scientists and of seeing the experimental procedure firsthand, and gives the scientists access to colleagues with a broader statistical training. The experience is usually highly rated by the student participants.

Classes at WSU meet four hours per week for ten weeks. A typical class involves about 10 students who are either in the applied statistics master’s degree program or who are undergraduates majoring in mathematics with a statistics concentration. Originally, two quarters (20 weeks) of probability and statistics formed the prerequisite, and the course covered much of Chapters 1–4, 6, 7, 10, 11, and 13, with Chapters 3 and 4 being primarily

